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RESEARCH ARTICLE

SENSITIVITY AND UNCERTAINTY ANALYSIS OF THE KEFF DUE TO JENDL4 CROSS SECTIONS UNCERTAINTIES OF THE ²³⁵U AND ²³⁸U ISOTOPES IN NUCLEAR REACTORS

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ABSTRACT

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Key words:

Cross Section, Sensitivity, Covariance Matrix, Nuclear Uncertainty, MCNP6. The main objective of this study is to estimate nuclear data uncertainties on the effective multiplication factor (Keff) related to elastic, inelastic, capture and fission cross sections and the correlations between them. Different rapid and thermal cases of the different IHECSBE benchmarks have been studied by using nuclear data evaluation JENDL4 to calculate the sensitivity vectors for ²³⁵U and ²³⁸U isotopes and four cases used to validate our sensitivity vectors. These sensitivity vectors are calculated by using the adjoint-weighted perturbation method based on the Kpert card of the Monte Carlo code MCNP6. Thus, the uncertainties induced by nuclear data have been calculated by combining the sensitivity vectors with the covariance matrices that are generated by the ERRORJ module of the recently updated of the nuclear data processing system NJOY99. In this study, we found the four cross sections (elastic, inelastic, capture and fission) of the ²³⁵U and their covariance matrices Lack the adjustement especially in the rapid energies. Against, the cross sections and covariance matrices of the ²³⁸U not lack the adjustement especially in the thermal energies.

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INTRODUCTION

Since the beginning of the century, the nuclear data evaluation communities are putting more and more attention to the assessment of uncertainties. This increased interest concerns both basic data (cross section, emission spectrum ...) and calculated quantities for large systems. Such as neutron multiplication factor Keff, reactivity, reaction rate and others. With the large availability of the covariance files, as in the JENDL4 (Shibata et al., 2011) nuclear data evaluation, more and more studies are started using this information to deduce target accuracies for neutronic parameters in future reactors and therefore future priorities for experimental measurements of differential data. Several probabilistic and deterministic codes are made for the analysis of the sensitivity and the uncertainties of the nuclear data on the integral nuclear parameters (SCALE, MCNP, KENO, DRAGON...). Most of these codes used the multigroup adjoint-weighted technique. Except MCNP6 (Pelowitz, 2011) computed the changes in a tally response (such as Keff-eigenvalue) by using the differential operator technique with continuous energy spectrum (McKinney and Iverson, 1996). Now, it compute the changes in reactivity strictly in Keff-eigenvalue problems by using the adjoint-weighted methodology with continuous

*Corresponding author: Kaddour, M. Radiations and Nuclear Systems Laboratory, University Abdelmalek Essaadi, Faculty of Sciences of Tetuan, Morocco. energy spectrum (Kiedrowski and Brown, 2011; Kiedrowski et al., 2011). The technique of differential operator considered the source of neutrons unperturbed (Kiedrowski and Brown, 2010). The sensitivity with continuous energy spectrum has no problem of the self shielding effect than the sensitivity with multigroup energy spectrum (LAVILLE, 2011; Williams and Rearden, 2008). For this, we used the adjoint-weighted technique with continuous energy spectrum to calculate the sensitivity profiles in this work. The sensitivity profiles and covariance matrices are combined in order to obtain final uncertainties (IVANOVA, 2011). Several sensitivities and uncertainties analysis for improving and adjusting the cross sections of the important isotopes in nuclear data evaluation JENDL4 and in simple and complex nuclear systems are done by different codes and different perturbation techniques (Augusto Hernández-Solís, 2012; Augusto Hernández-Solís et al., 2012). But, there are still errors on the integral nuclear parameters, they due especially to the JENDL4 cross sections uncertainties in the ²³⁵U. These errors are detected with the new adjoint-weighted technique of the MCNP6 code. In this work, a sensitivity and uncertainty analysis have been performed for certain cases of the different IHECSBE (International Handbook of Evaluated Criticality Safty Benchmark Experiments) (IHECSBE, 2007) benchmarks by using the MCNP6 and NJOY99 (MacFarlane, 2002) codes. Results of the uncertainty calculated by the adjoint-weighted theory and produced by elastic, inelastic, capture and fission

nuclear data on the multiplication factor are presented and analyzed.

Methodology and Study Approach

Adjoint-weighted Technique

Starting from the nuclear transport equation and applying a first-order perturbation, the following expression for the change in reactivity ρ can be derived (Kiedrowski and Brown, 2011):

$$\Delta \rho = -\frac{\langle \Psi^+, P\Psi \rangle}{\langle \Psi^+, F'\Psi \rangle} \tag{1}$$

The reactivity is related to Keff in the typical way:

$$\rho = \frac{(\text{Keff}-1)}{\text{Keff}}$$
(2)

The angular flux in the unperturbed system is and its adjoint is denoted by Ψ^+ . P is the operator for the perturbation taking the form:

$$\boldsymbol{P} = \frac{1}{t} - \boldsymbol{S} - \boldsymbol{\lambda} \boldsymbol{F}$$
(3)

The eigenvalue is:

$$=\frac{1}{\text{Keff}}$$
(4)

And the tree terms in P from left to right, are the change in the total cross section, the change in scattering operator, and the change in the fission multiplication operator. F' is the perturbed fission operator. Monte Carlo technique can be used to sample the numerator and the denominator in continuousenergy forward calculation (Kiedrowski and Brown, 2011) and the change in reactivity can be estimated by taking the ratio in (1). We express change in cross section as:

$$\sigma_x = f\sigma_x \tag{5}$$

We apply the relationship:

$$K_{eff} = K_{eff} \frac{K_{eff} \Delta \rho}{1 - K_{eff} \rho}$$
(6)

We compute sensitivity coefficients by:

$$S_{K_{eff}\sigma_{x}} = \frac{1}{f} \frac{K_{eff} \Delta \rho}{1 - K_{eff} \Delta \rho}$$
(7)

The quantity K_{eff} ρ scales linearly with f; can make arbitrarily small until sensitivity becomes sufficiently precise.

Study Approach

During this study:

We have selected different criticality safety cases of IHECSBE (IHECSBE, 2007) benchmarks. We have studied the impact of the cross sections uncertainties for ²³⁵U, and ²³⁸U isotopes on the effective multiplication factor uncertainty in each selected case. The selected isotopes are generally known by their important contribution in the effective multiplication factor calculation.

The sensitivity vectors for multiplication factor were generated by using Kpert card of MCNP6 code in 15 energy groups; they are represented in Table 1.

Table 1.	Fifteen	energy	groups	used	in ou	r sensi	tivity	and	uncert	ainty
				analy	sis					

Groups numbers	Energy groups (Mev)
1	0.00E 00 - 1.10E-07
2	1.10E-07 - 5.40E-07
3	5.40E-07 - 4.00E-06
4	4.00E-06 - 2.26E-05
5	2.26E-05 - 4.54E-04
6	4.54E-04 - 2.04E-03
7	2.04E-03 - 9.12E-03
8	9.12E-03 - 2.48E-02
9	2.48E-02 - 6.74E-02
10	6.74E-02 - 1.83E-01
11	1.83E-01 - 4.98E-01
12	4.98E-01 - 1.35E00
13	1.35E00 - 2.23E00
14	2.23E00 - 6.07E00
15	6.07E00 - 19.60E00

The covariance matrices generated by ERRORJ module of the NJOY99 (MacFarlane, 2002) processing system based on the same discretization of the sensitivity energy. The values of the covariance were computed for fifteen energy groups mentioned above by using a weighting flux that corresponds to the 1/E + fission spectrum + thermal maxwellian shape. For all cases, an infinite dilution condition was assumed ($\sigma_0 = 1 \cdot 10^{10}$ barns) and the temperature was considered to be 300 K. The steps adopted in this study are presented in Figure 1:

The perturbation approach is generally based on the NJOY99 processing system, the MCNP6 code and the program for calculating the total uncertainty produced by nuclear data on the Keff (Keff-nucl.).

Inputs are the MCNP6 input file and JENDL4 file containing the matrices of covariances. As shown in figure 1, JENDL4 file is processed by NJOY99 in order to produce cross sections in the ACE format and covariance matrices used by program for calculating on the Keff– nucl.

The sensitivity vectors were calculated by using the most commonly used radiation transport code MCNP6. The sensitivity profiles $S_{Keff\sigma_{xg}}$ are defined as the relative change in a response Keff (the effective multiplication factor) with respect to cross section σ_x in a particular energy group g, it is defined as:

$$S_{Keff\sigma_{x},g} = \frac{\sigma_{x,g}}{Keff} \frac{Keff}{\sigma_{x,g}} - \frac{1}{f} \frac{K_{eff}\Delta\rho}{1-K_{eff}\rho}$$
(8)

The sensitivity profile $S_{Keff\sigma_{xg}}$ is obtained by using the perturbation option of MCNP6 that is defined in Kpert card by using the first-order perturbation of the adjoint-weighted technique.

The cross sections were perturbed as described in the following steps:

1. Four cross sections will be considered: elastic, inelastic, capture and fission cross section, and only one specific cross section in one energy group and one isotope varied each time.



Fig. 1. flowchart of the uncertainty calculation by MCNP6 and NJOY99 codes

- 2. Then a material card is created in which the atomic density for the relevant isotope is increased by 1%.
- The Kpert card is then created specifying that: the relevant material is replaced by the perturbed material in each of the cells in which the material is present. Perturbation cards are given for all energy groups.
- 4. Finally, MCNP6 is run with this modification in the input; and in the output file a table is given with the results of different perturbations and their related statistical uncertainties.

These sensitivity vectors must be combined with covariances matrices (10) and (11), by using a program calculating Keff uncertainties in similar energy groups.

The total uncertainty is calculated by using the following equation [9]:

$$\frac{\lambda Keff}{Keff} = \sqrt{\sum_{i} \sigma_{x}} g \left[\frac{\lambda Keff}{Keff}\right]_{i,\sigma_{x},g}^{2}$$
(9)

i: index of material σ_x : index of reaction cross section g: index of energy group

The contribution of every nuclide-reaction in $\frac{\Delta Keff}{Keff}$ is calculated as follows [5]:

$$\left(\sqrt{S_{Keff,\sigma_{x,g}}cov(\sigma_{x,g},\sigma_{y,g})}S_{Keff,\sigma_{y,g}}\right)$$
(10)

$$\left(-\sqrt{\left|S_{Keff\sigma_{x,g}}cov(\sigma_{x,g},\sigma_{y,g'})S_{Keff\sigma_{y,g}}\right|}\right)$$
(11)

If $(S_{Keff,\sigma_{xg}}cov(\sigma_{x,g},\sigma_{y,g})S_{Keff,\sigma_{y,g}}) = 0)$, we have using the equation (10).

If $(S_{Keff,\sigma_{xg}}cov(\sigma_{xg},\sigma_{yg})S_{Keff,\sigma_{yg}} < 0)$, we have using the equation (11).

 $S_{Keff,\sigma_{x,g}}$: Sensitivity coefficient for Keff due to the neutron cross section σ_x , and energy group g.

 $cov(\sigma_{x,g}, \sigma_{y,g'})$: Covariance matrix that comprises covariance data for two cross sections (σ_x, σ_y) in the energy groups g and g'.

Effective Multiplication Factors Calculated by MCNP6

The K_{eff} values with their related standard deviations for the cases studied are listed in table 2. The third column represent values from the International Criticality Safty Benchmark experements (IHECSBE). Our results calculated by MCNP6 code and JENDL4 nuclear data evaluation are represented in the second column. We chose these cases because their relative differences between the experimental Keff and the calculated Keff are higher than their experimental uncertainties and their standard deviations.

 Table 2. calculated and experimental Keff of the cases of the benchmarks and theirs standard deviations and experimental uncertainties

Cases of benchmarks	ins and experimental uncertain	ncertainties		
	Keff ± std.dedev ¹ Keff ± (MCNP6)) (HEC	$\frac{\text{Keff} \pm \Delta \text{Keff}^2}{(\text{IHECSBE})}$		
HEU-MET-FAST-001-001 (hmf001-001)	0.99743 ± 0.00025	1.00000 ± 0.0010		
HEU-MET-FAST-004-001 (hmf004-001)	1.00009 ± 0.00022	0.99850 ± 0.0000		
HEU-MET-FAST-008-001 (hmf008-001)	$0.99285 \!\pm\! 0.00018$	0.9989 ± 0.0016		
HEU-MET-FAST -015-001 (hmf015-001)	0.99252 ± 0.00020	0.9996 ± 0.0017		
HEU-SOL-THERM-006-001 (hst006-001)	0.98360 ± 0.00033	0.9973 ± 0.0050		
HEU-SOL-THERM-013-001 (hst013-001)	0.99911 ± 0.00022	1.0012 ± 0.0026		
HEU-SOL-THERM-016-001 (hst016-001)	0.99117 ± 0.00036	1.00000 ± 0.0036		
HEU-SOL-THERM-028-001 (hst028-001)	0.99623 ± 0.00031	1.00000 ± 0.0023		
HEU-SOL-THERM-035-007 (hst035-007)	1.00430 ± 0.00033	1.00000 ± 0.0035		
HEU-SOL-THERM-037-001 (hst037-001)	1.00980 ± 0.00026	0.99800 ± 0.0034		

¹this uncertainty means the statistical uncertainty or standard deviation in MCNP6 calculated with the Monte Carlo technique.

² this uncertainty means the experimental uncertainty due to uncertainties in critical heights, uncertainties in solution constituents, and in isotropic constituents (IHECSBE, 2007).

Validation of Sensitivity Results

The calculation of the sensitivities coefficients by the adjointweighted technique is new in the code MCNP6; for this, we compared the results of this technique with the results of the old technique in MCNP code (differential operator technique) and with the sensitivities coefficients which are in IHECSBE and calculated by the KENO code. Also, we compared the results of the adjoint-weighted technique between tree nuclear data evaluations ENDFB/VI.8, ENDFB/VII.0 (Chadwick *et al.*, 2006) and JENDL-4.0. This comparison is used in 30 energy groups; they are represented in Table 3.

Table 3. Thirty energy groups used in our sensitivity validation

Groups numbers	Energy groups (Mev)
1	0.00E+0 - 1.00E-02
2	1.00E-02 -2.15E-02
3	2.15E-02 - 4.64E-02
4	4.64E-02 - 1.00E-01
5	1.00E-01 - 2.15E-01
6	2.15E-01 - 4.64E-01
7	4.64E-01 - 1.00E+00
8	1.00E+00 - 2.15E+00
9	2.15E+00 - 4.64E+00
10	4.64E+00 - 1.00E+01
11	1.00E+01 - 2.15E+01
12	2.15E+01 - 4.64E+01
13	4.64E+01 - 1.00E+02
14	1.00E+02 - 2.15E+02
15	2.15E+02 - 4.64E+02
16	4.64E+02 - 1.00E+03
17	1.00E+03 - 2.15E+03
18	2.15E+03 - 4.64E+03
19	4.64E+03 - 1.00E+04
20	1.00E+04 - 2.15E+04
21	2.15E+04 - 4.64E+04
22	4.64E+04 - 1.00E+05
23	1.00E+05 - 2.00E+05
24	2.00E+05 - 4.00E+05
25	4.00E+05 - 8.00E+05
26	8.00E+05 - 1.40E+06
27	1.40E+06 - 2.50E+06
28	2.50E+06 - 4.00E+06
29	4.00E+06 - 6.50E+06
30	6.50E+06 - 6.50E+06

0.14 0.12 sensitivities % / % 0.10 0.08 0.06 0.04 0.02 0.00 -0.02 0 5 10 15 20 30 25 35 energy groups

Sensitivities of ²³⁵U elastic scattering cross section

The Figures below show the results of the sensitivity validation in rapid experiment: Godiva (highly enriched uranium sphere), hmf004-001 and hmf018-001, and in thermal experiment hst001-001; for four reactions: elastic and inelastic scattering, capture and fission.

The differences between the results of sensitivities in the above Figures (2, 3, 4, 5) are due to:

- The difference between the nuclear data evaluation used.

- The difference between the perturbation techniques used: in the differential operator technique, the fundamental eigenfuction (fission distribution) approximated as unperturbed.

– The absence of thermal neutron scattering: $S(\alpha, \beta)$ in the KENO code.

- The difference between the two codes: MCNP6 uses continuous energy, KENO uses multigroup energy. In general, the adjoint-weighted technique has the same allure with other technique. Then, it is validated.

Uncertainty Analysis

Uncertainty on the Keff Produced by the Nuclear Data Uncertainties of the ²³⁵U

Figure 6 shows the effect of cross sections uncertainties related to 235 U isotope on the effictive multiplication factor (nucl. uncert. on Keff or Keff-nucl.) in different nuclear experiences. The uncertainties on the Keff produced by elastic, inelastic scattering, capture and fission cross sections and the effect of the correlation between them are represented by adjoint-weighted technique and by pcm (1pcm = 10^{-5})

Interpretations and Conclusions on the Results of ²³⁵U

– The elastic, inelastic, capture and fission cross sections and the correlations between them for 235 U in the rapid experiences, they have large contribution of uncertainties in the effective multiplication factor uncertainties (Keff-nucl.). Then, these four cross sections and their covariance matrices in 235 U require the adjustment in the rapid energies.



Sensitivities of ²³⁵U inelastic scattering cross section





Fig. 2. Sensitivities of ²³⁵U elastic and inelastic scattering, capture and fission cross sections in Godiva



Sensitivities of ²³⁵U elastic scattering cross section



Sensitivities of ²³⁵U inelastic scattering cross section





Fig. 3. Sensitivities of ²³⁵U elastic and inelastic scattering, capture and fission cross sections in hmf004-001



Fig 4. Sensitivities of ²³⁵U elastic and inelastic scattering, capture and fission cross sections in hmf018-001

















Fig. 7. Uncertainties (pcm) produced by different cross sections of ²³⁸U for different experiences

– The elastic, inelastic, capture and fission cross sections uncertainties and the correlations between them for ²³⁵U in the thermal experiences, they have small contribution of uncertainties in the effective multiplication factor uncertainties (Keff-nucl.) than its contribution of uncertainties in Keff-nucl of the rapid experiences. But, in another study we found

Keff-nucl. increases with small increase in the atomic density for 235 U in six cases of hst001 (Kaddour *et al.*, 2013). Thus, we cannot assure the accuracy of these cross sections and their covariances matrices in the thermal energies when the 235 U atomic density increases.

Uncertainty on the Keff Produced by the Nuclear Data Uncertainties of the ²³⁸U

Figure 7 shows the effect of cross sections uncertainties related to 238 U isotope on the effictive multiplication factor (nucl. uncert. on Keff or Keff-nucl.) in different nuclear experiences. The uncertainties on the Keff produced by elastic, inelastic scattering, capture and fission cross sections and the effect of the correlation between them are represented by adjoint-weighted technique and by pcm (1pcm = 10^{-5}).

Interpretations and Conclusions on the Results of ²³⁸U

– The effect of elastic, inelastic, capture and fission cross sections uncertainties related to 238 U on the effictive multiplication factor uncertainties is very small in the thermal experiences than the rapid experiences; and that is due to the small contribution of 238 U cross sections on the Keff in the thermal energies. Then, in this study, we can conclude that: these cross sections and their covariance matrices do not lack the adjustment in the thermal energies.

– In another study we found Keff-nucl. increases with the increase in the 238 U atomic density in six cases of hst001 (Kaddour *et al.*, 2013). Thus, we cannot assure the accuracy of these cross sections and their covariance matrices in the rapid energies when the atomic density of the 238 U increases.

Conclusion

In this work we have analysed the sensitivities and uncertainties on the effictive multiplication factor (Keff) produced by JENDL4 nuclear data; espicially the elastic and inelastic scattering, capture and fission cross sections and their correlations in the ²³⁵U and ²³⁸U by the adjoint- weigted technique of the MCNP6 code. Firstly, we validated our perturbation technique in four experiences. After, a series of critical experiences have been studied by using the Monte Carlo code MCNP6 and the ERRORJ module of the last update NJOY99 to calculate the sensitivities vectors and to process the covariance matrices. In the end, the sensitivity vectors and covariance matrices are combined in order to obtain final uncertainties. As a conclusins:

– The four cross sections (elastic, inelastic, capture and fission) of the 235 U and their covariance matrices Lack the adjustment especially in the rapid energies.

– The cross sections and covariance matrices of the 238 U not lack the adjustement especially in the thermal energies.

The adjustment of these cross sections and their covariance matrices is our aim in our future works.

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